

Title: Seidl: Virtual_Machines (21.04.2015)

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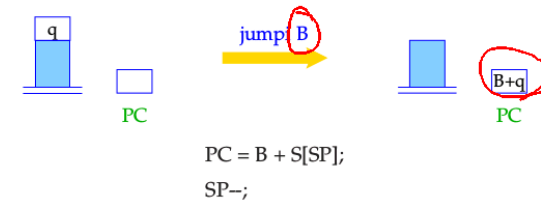
Duration: 88:06 min

Pages: 32

4.5 The switch-Statement

Idea:

- Multi-target branching in **constant time!**
- Use a **jump table**, which contains at its i -th position the jump to the beginning of the i -th alternative.
- Realized by **indexed jumps**.



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Simplification:

We only regard switch-statements of the following form:

```

s ≡ switch (e) {
  case 0: ss0 break;
  case 1: ss1 break;
  ⋮
  case k - 1: ssk-1 break;
  default: ssk
}
    
```

s is then translated into the instruction sequence:

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```

code s ρ = codeR e ρ      C0: code ss0 ρ      B: jump C0
           check 0 k B    jump D
           ⋮
           ⋮              ⋮
           Ck: code ssk ρ  D: ⋮
           jump D
    
```

jump B

- The Macro **check 0 k B** checks, whether the R-value of e is in the interval $[0, k]$, and executes an indexed jump into the table **B**
- The jump table contains direct jumps to the respective alternatives.
- At the end of each alternative is an unconditional jump out of the **switch-statement**.

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```

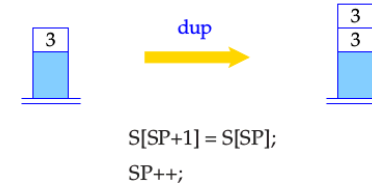
check 0 k B = dup      dup      jumpi B
              loadc 0   loadc k   A: pop
              geq      le        loadc k
              jumpz A   jumpz A   jumpi B

```

jump (B+2)

- The R-value of e is still needed for indexing after the comparison. It is therefore copied before the comparison.
- This is done by the instruction `dup`.
- The R-value of e is replaced by k before the indexed jump is executed if it is less than 0 or greater than k .

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```

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          check 0 k B

```

$C_0:$
 $code_{SS_0} \rho$
 $jump D$
 \dots
 $C_k:$
 $code_{SS_k} \rho$
 $jump D$

$B:$
 $jump C_0$
 \dots
 $jump C_k$
 $D:$
 \dots

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Note:

- The jump table could be placed directly after the code for the Macro `check`. This would save a few unconditional jumps. However, it may require to search the `switch`-statement twice.
- If the table starts with u instead of 0, we have to decrease the R-value of e by u before using it as an index.
- If all potential values of e are **definitely** in the interval $[0, k]$, the macro `check` is not needed.

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5 Storage Allocation for Variables

Goal:

Associate **statically**, i.e. at compile time, with each variable x a fixed (relative) address ρx

Assumptions:

- variables of basic types, e.g. `int`, ... occupy one storage cell.
- variables are allocated in the store in the order, in which they are declared, starting at address 1.

Consequently, we obtain for the declaration $d \equiv t_1 x_1; \dots t_k x_k;$ (t_i basic type) the address environment ρ such that

$$\rho x_i = i, \quad i = 1, \dots, k$$

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We need a function `sizeof` (notation: $|\cdot|$), computing the space requirement of a type:

$$|t| = \begin{cases} 1 & \text{if } t \text{ basic} \\ k \cdot |t'| & \text{if } t \equiv t'[k] \end{cases}$$

Accordingly, we obtain for the declaration $d \equiv t_1 x_1; \dots t_k x_k;$

$$\begin{aligned} \rho x_1 &= 1 \\ \rho x_i &= \rho x_{i-1} + |t_{i-1}| \quad \text{for } i > 1 \end{aligned}$$

Since $|\cdot|$ can be computed at compile time, also ρ can be computed at compile time.

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5.1 Arrays

Example `int [11] a;`

The array a consists of 11 components and therefore needs 11 cells. ρa is the address of the component $a[0]$.



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Task:

Extend `codeL` and `codeR` to expressions with accesses to array components.

Be $t[c] a;$ the declaration of an array a .

To determine the start address of a component $a[i]$, we compute $\rho a + |t| * (R\text{-value of } i)$.

In consequence:

$$\begin{aligned} \text{code}_L a[e] \rho &= \text{loadc } (\rho a) \\ &\quad \text{code}_R e \rho \\ &\quad \text{loadc } |t| \\ &\quad \text{mul} \\ &\quad \text{add} \end{aligned}$$

... or more general:

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$$\text{code}_L e_1[e_2] \rho = \text{code}_R e_1 \rho$$

$$\text{code}_R e_2 \rho$$

$$\text{loadc } |t|$$

$$\text{mul}$$

$$\text{add}$$

Remark:

- In **C**, an array is a **pointer**. A declared array a is a **pointer-constant**, whose R-value is the start address of the array.
- Formally, we define for an array e : $\text{code}_R e \rho = \text{code}_L e \rho$
- In **C**, the following are equivalent (as L-values):

$$2[a] \quad a[2] \quad a + 2$$

Normalization: Array names and expressions evaluating to arrays occur in front of index brackets, index expressions inside the index brackets.

a + 2

$$\text{code}_L e_1[e_2] \rho = \text{code}_R e_1 \rho$$

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5.2 Structures

In **Modula** and **Pascal**, structures are called **Records**.

Simplification:

Names of structure components are not used elsewhere. Alternatively, one could manage a separate environment ρ_{st} for each structure type st .

Be $\text{struct } \{ \text{int } a; \text{int } b; \} x;$ part of a declaration list.

- x has as relative address the address of the first cell allocated for the structure.
- The components have addresses **relative** to the start address of the structure. In the example, these are $a \mapsto 0, b \mapsto 1$.

Let $t \equiv \text{struct } \{ t_1 c_1; \dots t_k c_k \}$. We have

$$|t| = \sum_{i=1}^k |t_i|$$

$$\rho c_1 = 0 \quad \text{and}$$

$$\rho c_i = \rho c_{i-1} + |t_{i-1}| \quad \text{for } i > 1$$

We thus obtain:

$$\text{code}_L (e.c) \rho = \text{code}_L e \rho$$

$$\text{loadc } (\rho c)$$

$$\text{add}$$

Example

Be `struct { int a; int b; } x;` such that $\rho = \{x \mapsto 13, a \mapsto 0, b \mapsto 1\}$.

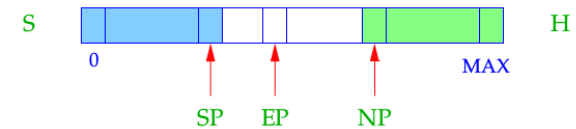
This yields:

```
codeL(x.b) ρ = loadc 13
                loadc 1
                add
```

6 Pointer and Dynamic Storage Management

Pointer allow the access to anonymous, dynamically generated objects, whose life time is not subject to the LIFO-principle.

⇒ We need another potentially unbounded storage area H – the Heap.



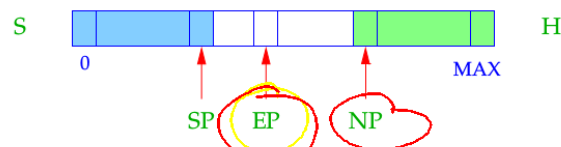
NP ≐ New Pointer; points to the lowest occupied heap cell.

EP ≐ Extreme Pointer; points to the uppermost cell, to which SP can point (during execution of the actual function).

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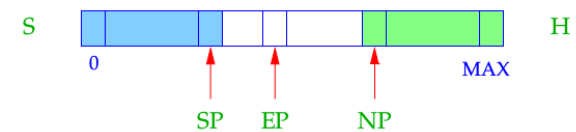
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NP ≐ New Pointer; points to the lowest occupied heap cell.

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Idea:

- Stack and Heap grow toward each other in S, but must not collide. (Stack Overflow).
- A collision may be caused by an increment of SP or a decrement of NP.
- EP saves us the check for collision at the stack operations.
- The checks at heap allocations are still necessary.

What can we do with pointers (pointer values)?

- set a pointer to a storage cell,
- dereference a pointer, access the value in a storage cell pointed to by a pointer.

There are two ways to set a pointer:

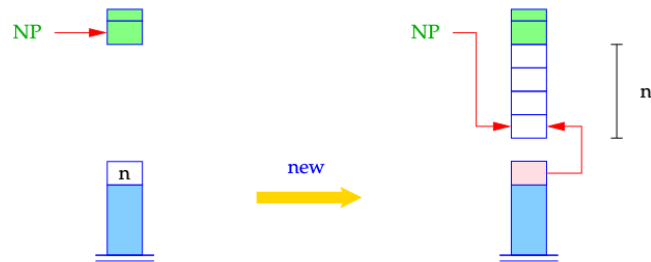
- A call `malloc(e)` reserves a heap area of the size of the value of `e` and returns a pointer to this area:

$$\text{code}_R \text{ malloc}(e) \rho = \text{code}_R e \rho$$

`new`

- The application of the address operator `&` to a variable returns a pointer to this variable, i.e. its address ($\hat{=}$ L-value). Therefore:

$$\text{code}_R (\&e) \rho = \text{code}_L e \rho$$



```

if (NP - S[SP] ≤ EP)
    S[SP] = NULL;
else {
    NP = NP - S[SP];
    S[SP] = NP;
}

```

- NULL is a special pointer constant, identified with the integer constant 0.
- In the case of a collision of stack and heap the NULL-pointer is returned.

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Handwritten mark: a circled 'e' followed by an 'X'.

Dereferencing of Pointers:

The application of the operator `*` to the expression e returns the **contents** of the storage cell, whose address is the R-value of e :

$$\text{code}_L(*e) \rho = \text{code}_R e \rho$$

Example

Given the declarations

```
struct t { int a[7]; struct t *b; };
int i, j;
struct t *pt;
```

and the expression $((pt \rightarrow b) \rightarrow a)[i + 1]$

Because of $e \rightarrow a \equiv (*e).a$ holds:

$$\begin{aligned} \text{code}_L(e \rightarrow a) \rho &= \text{code}_R e \rho \\ &\quad \text{loadc}(\rho a) \\ &\quad \text{add} \end{aligned}$$

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- **dereference** a pointer, access the value in a storage cell pointed to by a pointer.

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- (1) A call `malloc(e)` reserves a heap area of the size of the value of e and returns a pointer to this area:

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`int x[5];`

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