

Script generated by TTT

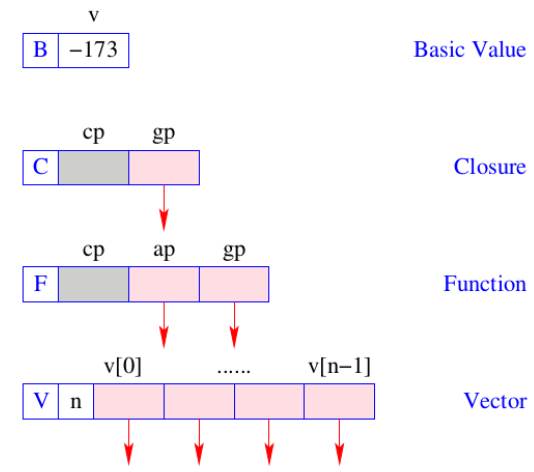
Title: Seidl: Virtual Machines (05.05.2014)

Date: Mon May 05 10:17:42 CEST 2014

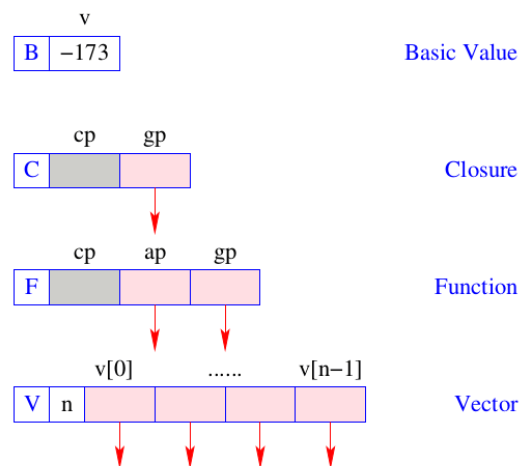
Duration: 89:31 min

Pages: 43

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The instruction `new (tag, args)` creates a corresponding object (B, C, F, V) in **H** and returns a reference to it.

We distinguish three different kinds of code for an expression e :

- `codev e` — (generates code that) computes the **V**alue of e , stores it in the heap and returns a reference to it on top of the stack (the normal case);
- `codeB e` — computes the value of e , and returns it on the top of the stack (only for **B**asic types);
- `codeC e` — does **not** evaluate e , but stores a **C**losure of e in the heap and returns a reference to the closure on top of the stack.

We start with the code schemata for the first two kinds:

13 Simple expressions

Expressions consisting only of constants, operator applications, and conditionals are translated like expressions in imperative languages:

$$\begin{aligned}
 \text{code}_B b \rho \text{sd} &= \text{loadc } b \\
 \text{code}_B (\square_1 e) \rho \text{sd} &= \text{code}_B e \rho \text{sd} \\
 &\quad \text{op}_1 \\
 \text{code}_B (e_1 \square_2 e_2) \rho \text{sd} &= \text{code}_B e_1 \rho \text{sd} \\
 &\quad \text{code}_B e_2 \rho (\text{sd} + 1) \\
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$$\begin{aligned}
 \text{code}_B (\text{if } e_0 \text{ then } e_1 \text{ else } e_2) \rho \text{sd} &= \text{code}_B e_0 \rho \text{sd} \\
 &\quad \text{jump } A \\
 &\quad \text{code}_B e_1 \rho \text{sd} \\
 &\quad \text{jump } B \\
 &\quad A: \text{code}_B e_2 \rho \text{sd} \\
 &\quad B: \dots
 \end{aligned}$$

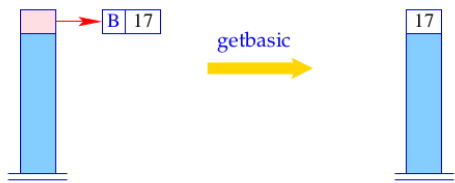
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Note:

- ρ denotes the actual **address environment**, in which the expression is translated.
- The extra argument **sd**, the **stack difference**, *simulates* the movement of the **SP** when instruction execution modifies the stack. It is needed later to address variables.
- The instructions **op₁** and **op₂** implement the operators \square_1 and \square_2 , in the same way as the operators **neg** and **add** implement negation resp. addition in the **CMa**.
- For all other expressions, we first compute the value in the heap and then dereference the returned pointer:

$$\begin{aligned}
 \text{code}_B e \rho \text{sd} &= \text{code}_V e \rho \text{sd} \\
 &\quad \text{getbasic}
 \end{aligned}$$

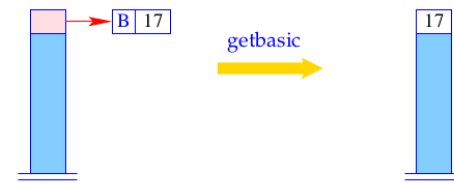
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```

if (H[S[SP]] != (B, ...))
    Error "not basic!";
else
    S[SP] = H[S[SP]].v;

```



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For `codev` and simple expressions, we define analogously:

```

codev b ρ sd = loadc b; mkbasic
codev (□1 e) ρ sd = codeB e ρ sd
                  op1; mkbasic
codev (e1 □2 e2) ρ sd = codeB e1 ρ sd
                  codeB e2 ρ (sd + 1)
                  op2; mkbasic
codev (if e0 then e1 else e2) ρ sd = codeB e0 ρ sd
                  jumpz A
                  codev e1 ρ sd
                  jump B
                  A: codev e2 ρ sd
                  B: ...

```



```

S[SP] = new (B,S[SP]);

```

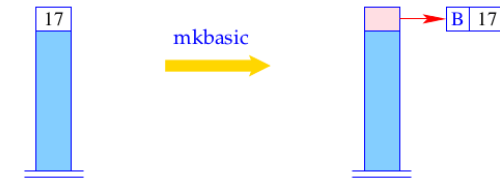
For `codeV` and simple expressions, we define analogously:

```

codeV b ρ sd           =   loadc b; mkbasic
codeV (□1 e) ρ sd       =   codeB e ρ sd
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                           codeB e2 ρ (sd + 1)
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codeV (if e0 then e1 else e2) ρ sd = codeB e0 ρ sd
                                       jumpz A
                                       codeV e1 ρ sd
                                       jump B
                                       A: codeV e2 ρ sd
                                       B: ...

```

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$S[SP] = \text{new}(B, S[SP]);$

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14 Accessing Variables

We must distinguish between **local** and **global** variables.

Example: Regard the function f :

```

let c = 5
in let f = fun a → let b = a * a
                    in b + c
    f c

```

The function f uses the **global** variable c and the **local** variables a (as formal parameter) and b (introduced by the inner **let**).

The binding of a global variable is determined, when the function is **constructed** (**static scoping!**), and later only looked up.

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Accessing Global Variables

- The bindings of global variables of an expression or a function are kept in a vector in the heap (**Global Vector**).
- They are addressed consecutively starting with 0.
- When an F-object or a C-object are constructed, the Global Vector for the function or the expression is determined and a reference to it is stored in the gp-component of the object.
- During the evaluation of an expression, the (**new**) register **GP** (Global Pointer) points to the actual Global Vector.
- In contrast, local variables should be administered on the stack ...

⇒ General form of the address environment:

$$\rho : \text{Vars} \rightarrow \{L, G\} \times \mathbb{Z}$$

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Accessing Local Variables

Local variables are administered on the stack, in **stack frames**.

Let $e \equiv e' e_0 \dots e_{m-1}$ be the application of a function e' to arguments e_0, \dots, e_{m-1} .

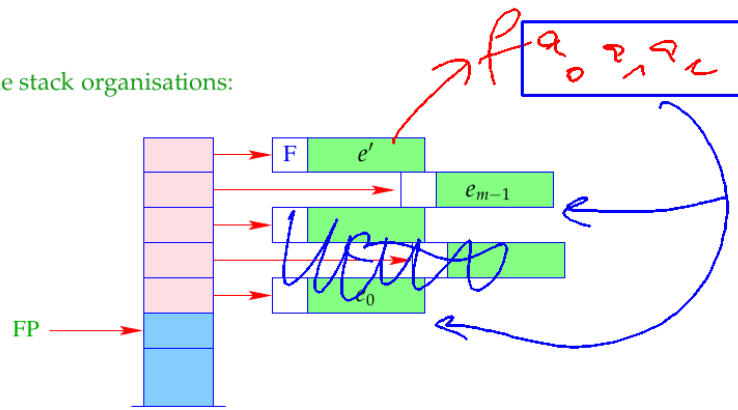
Warning:

The arity of e' does not need to be m :-)

- f may therefore receive less than n arguments (**under supply**);
- f may also receive more than n arguments, if t is a **functional type** (**over supply**).

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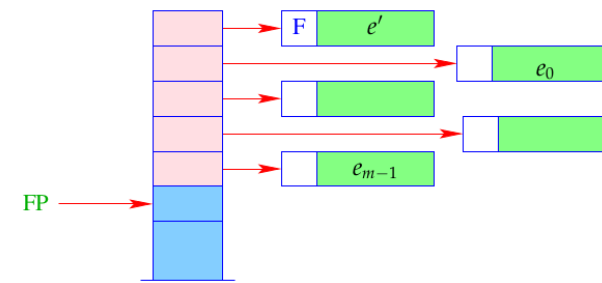
Possible stack organisations:



- + Addressing of the arguments can be done relative to **FP**
- The local variables of e' cannot be addressed relative to **FP**.
- If e' is an n -ary function with $n < m$, i.e., we have an over-supplied function application, the remaining $m - n$ arguments will have to be shifted.

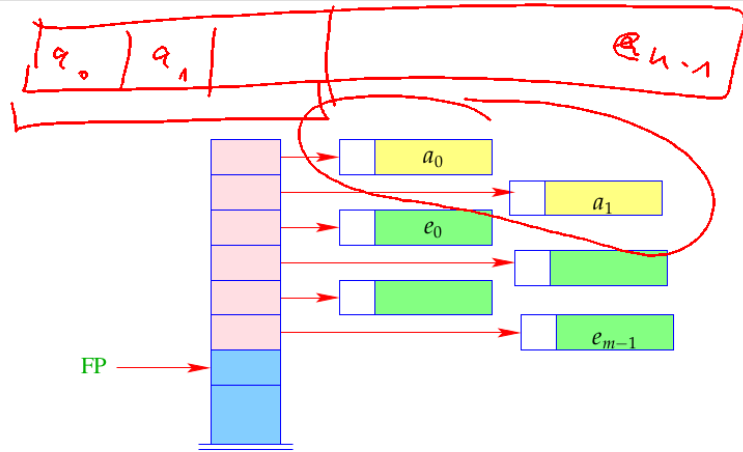
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Alternative:

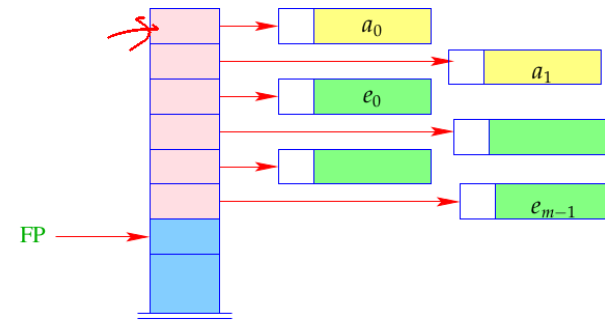


- + The further arguments a_0, \dots, a_{k-1} and the local variables can be allocated above the arguments.

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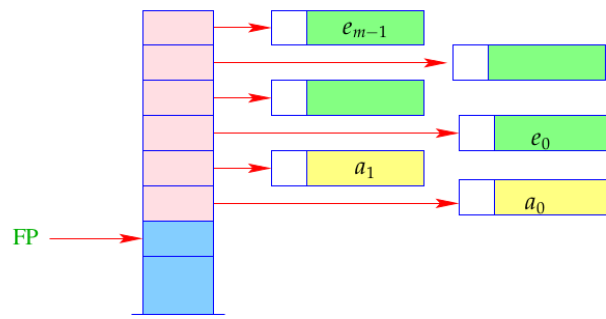


- Addressing of arguments and local variables relative to FP is no more possible. (Remember: m is unknown when the function definition is translated.)



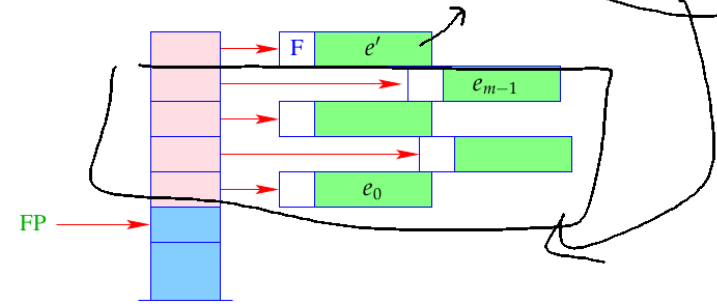
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- If e' evaluates to a function, which has already been partially applied to the parameters a_0, \dots, a_{k-1} , these have to be sneaked in underneath e_0 :

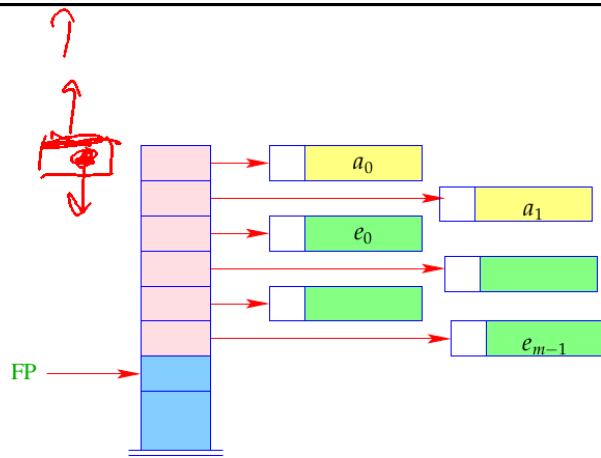


Possible stack organisations:

let $g = f(a_0, a_1, a_2)$



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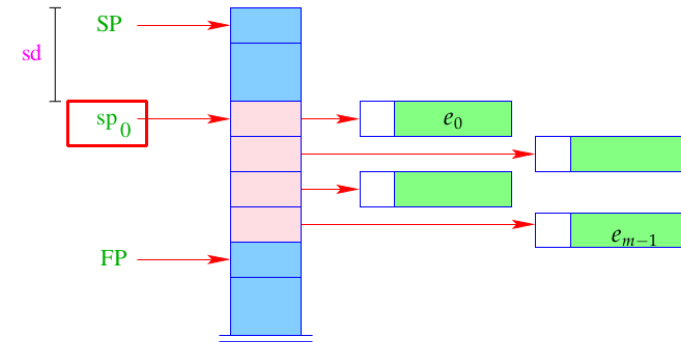


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Way out:

- We address both, arguments and local variables, relative to the stack pointer SP !!!
- However, the stack pointer changes during program execution...



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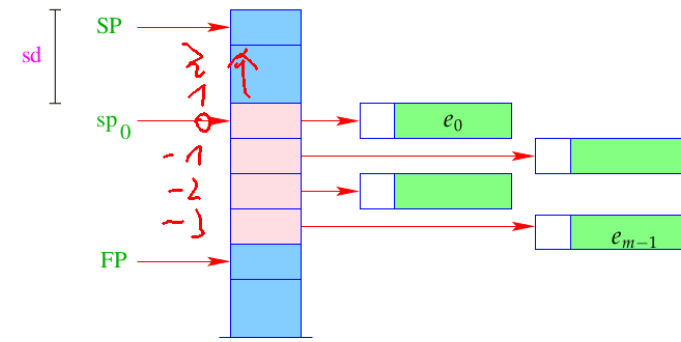
- The difference between the **current** value of SP and its value sp_0 at the entry of the function body is called the stack distance, sd .
- Fortunately, this stack distance can be determined at compile time for each program point, by **simulating the movement** of the SP.
- The formal parameters x_0, x_1, x_2, \dots successively receive the **non-positive** relative addresses $0, -1, -2, \dots$, i.e., $\rho x_i = (L, -i)$.
- The **absolute** address of the i -th formal parameter consequently is

$$sp_0 - i = (SP - sd) - i$$
- The local **let**-variables y_1, y_2, y_3, \dots will be successively pushed onto the stack:

123

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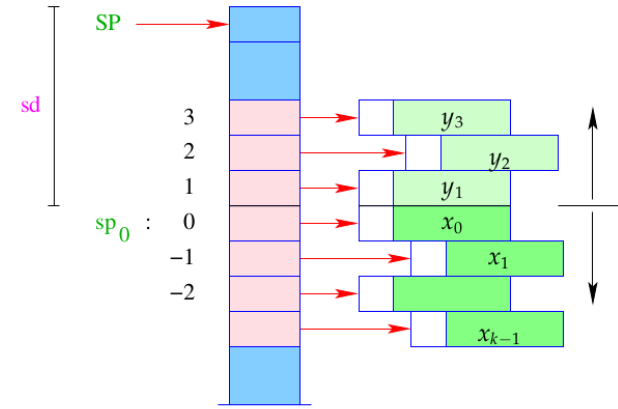
122

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$$sp_0 + i = (SP - sd) + i$$

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- The y_i have **positive** relative addresses $1, 2, 3, \dots$, that is: $\rho y_i = (L, i)$.
- The absolute address of y_i is then $sp_0 + i = (SP - sd) + i$

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With **CBN**, we generate for the access to a variable:

```
codeV x ρ sd = getvar x ρ sd
              eval
```

The instruction **eval** checks, whether the value has already been computed or whether its evaluation has to yet to be done (\implies will be treated later :-)

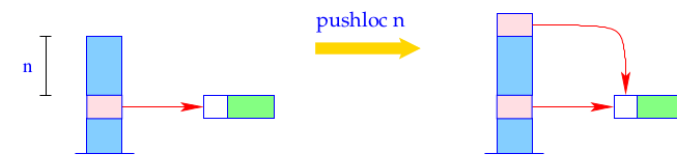
With **CBV**, we can just delete **eval** from the above code schema.

The (compile-time) macro **getvar** is defined by:

```
getvar x ρ sd = let (L i) = ρ x in
                match t with
                (L) → pushloc (sd - i)
                | G → pushglob i
                end
```

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The access to local variables:



$S[SP+1] = S[SP - n]; SP++;$

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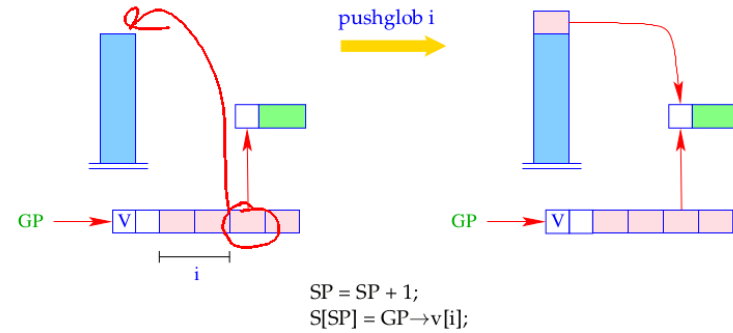
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                end
```

$$SP - (sd - i) = (SP - sd) + i$$

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The access to global variables is much simpler:



SP = SP + 1;
S[SP] = GP → v[i];

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Correctness argument:

Let **sp** and **sd** be the values of the stack pointer resp. stack distance before the execution of the instruction. The value of the local variable with address *i* is loaded from $S[a]$ with

$$a = sp - (sd - i) = (sp - sd) + i = sp_0 + i$$

... exactly as it should be :-)

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With **CBN**, we generate for the access to a variable:

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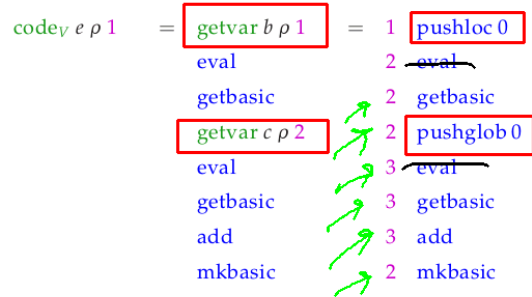
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```

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Example:

Regard $e \equiv (b + c)$ for $\rho = \{b \mapsto (L, 1), c \mapsto (G, 0)\}$ and $sd = 1$.

With CBN, we obtain:



15 let-Expressions

As a warm-up let us first consider the treatment of local variables :-)

Let $e \equiv \text{let } y_1 = e_1 \text{ in } \dots \text{let } e_n \text{ in } e_0$ be a nested **let**-expression.

The translation of e must deliver an instruction sequence that

- allocates local variables y_1, \dots, y_n ;
- in the case of
 - CBV: evaluates e_1, \dots, e_n and binds the y_i to their values;
 - CBN: constructs closures for the e_1, \dots, e_n and binds the y_i to them;
- evaluates the expression e_0 and returns its value.

Here, we consider the **non-recursive** case only, i.e. where y_j only depends on y_1, \dots, y_{j-1} . We obtain for CBN:

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```

codeV e ρ sd = codeC e1 ρ sd
                codeC e2 ρ1 (sd + 1)
                ...
                codeC en ρn-1 (sd + n - 1)
                codeV e0 ρn (sd + n)
                slide n // deallocates local variables

```

where $\rho_j = \rho \oplus \{y_i \mapsto (L, sd + i) \mid i = 1, \dots, j\}$.

In the case of **CBV**, we use `codeV` for the expressions e_1, \dots, e_n .

Warning!

All the e_i must be associated with the same binding for the global variables!

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$a \mapsto (L, 1)$
 $b \mapsto (L, 2)$

Example:

Consider the expression

$e \equiv \text{let } a = 19 \text{ in let } b = a * a \text{ in } a + b$

for $\rho = \emptyset$ and $sd = 0$. We obtain (for **CBV**):

0	loadc 19	3	getbasic	3	pushloc 1
1	mkbasic	3	mul	4	getbasic
1	pushloc 0	2	mkbasic	4	add
2	getbasic	2	pushloc 1	3	mkbasic
2	pushloc 1	3	getbasic	3	slide 2

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```

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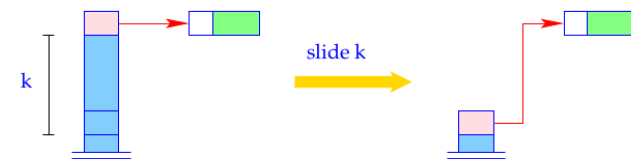
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The instruction `slide k` deallocates again the space for the locals:



$S[SP-k] = S[SP];$
 $SP = SP - k;$

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