Script generated by TTT

Title: Seidl: Virtual_Machines (10.07.2012)

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Pages: 46

Let us first consider the unifcation code for atoms and variables only:

Discussion:

- The translation of an equation $\tilde{X} = t$ is very simple :-)
- Often the constructed cells immediately become garbage :-(

Idea 2:

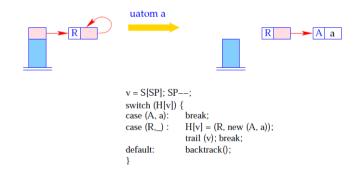
- Push a reference to the run-time binding of the left-hand side onto the stack.
- Avoid to construct sub-terms of t whenever possible!
- Translate each node of *t* into an instruction which performs the unifcation with this node !!

$$code_G (\tilde{X} = t) \rho = put \tilde{X} \rho$$

 $code_U t \rho$

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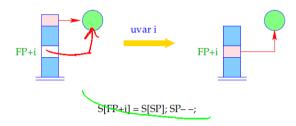
The instruction uatom a implements the unification with the atom a:



- The run-time function trail() records the a potential new binding.
- The run-time function backtrack() initiates backtracking.

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The instruction uvar i implements the unification with an un-initialized variable:



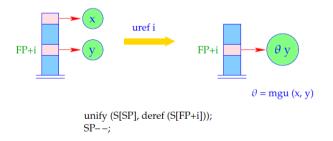
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The instruction pop implements the unification with an anonymous variable. It always succeeds :-)



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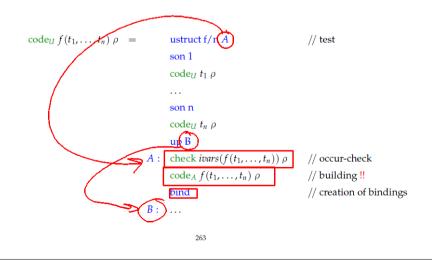
The instruction uref i implements the unification with an initialized variable:



It is only here that the run-time function unify() is called :-)

• The unification code performs a pre-order traversal over *t*.

 In case, execution hits at an unbound variable, we switch from checking to building :-)





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$$\lim_{t \to \infty} f(t_1, \dots, t_n) \rho = \operatorname{ustruct} f/n A$$

$$\operatorname{code}_{U} f(t_{1}, \ldots, t_{n}) \rho =$$
 usti

$$son 1$$
 $code_U t_1 \rho$

$$\operatorname{son} \operatorname{n} \operatorname{code}_{U} t_{n} \rho$$

up B

A: Check ivars
$$(f(t_1,...,t_n)) \rho$$
 $code_A f(t_1,...,t_n) \rho$

$$(t_n) \rho$$
 // occur-check $(t_n) \rho$ // building !!

// creation of bindings

// test

$$B: \ldots$$

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The Building Block:

Before constructing the new (sub-) term t' for the binding, we must exclude that it contains the variable X' on top of the stack !!!

This is the case iff the binding of no variable inside t' contains (a reference to) X'.

ivars(t') returns the set of already initialized variables of t.

The macro check $\{Y_1, \dots, Y_d\}$ ρ generates the necessary tests on the variables Y_1, \ldots, Y_d :

$$\text{check } \{Y_1, \dots, Y_d\} \ \rho = \text{check } (\rho \ Y_1)$$

$$\text{check } (\rho \ Y_2)$$

$$\dots$$

$$\text{check } (\rho \ Y_d)$$

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$$\begin{array}{lll} \operatorname{check} \left\{ Y_1, \dots, Y_d \right\} \, \rho & = & \operatorname{check} \left(\rho \, Y_1 \right) \\ & & \operatorname{check} \left(\rho \, Y_2 \right) \\ & & \dots \\ & & \operatorname{check} \left(\rho \, Y_d \right) \end{array}$$

The instruction check i checks whether the (unbound) variable on top of the stack occurs inside the term bound to variable i.

If so, unification fails and backtracking is caused:

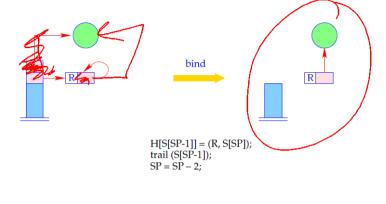


if (!check (S[SP], deref S[FP+i])) backtrack();

- ullet The unification code performs a pre-order traversal over t.
- In case, execution hits at an unbound variable, we switch from checking to building :-)

```
code_U f(t_1,\ldots,t_n) \rho =
                                    ustruct f/n A
                                                                      // test
                                    son 1
                                    code_U t_1 \rho
                                    son n
                                    code_U t_n \rho
                                    up B
                             A: check ivars(f(t_1, ..., t_n)) \rho
                                                                      // occur-check
                                    code_A f(t_1, \ldots, t_n) \rho
                                                                      // building !!
                                    bind
                                                                      // creation of bindings
                              B: ...
                                          263
```

The instruction bind terminates the building block. It binds the (unbound) variable to the constructed term:



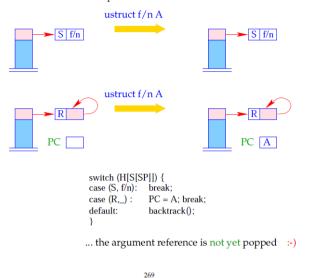
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The Pre-Order Traversal:

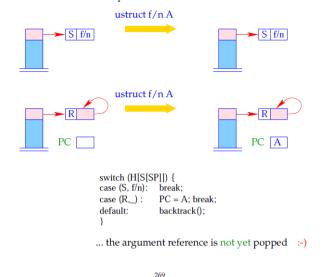
- First, we test whether the topmost reference is an unbound variable. If so, we jump to the building block.
- \bullet Then we compare the root node with the constructor f/n.
- Then we recursively descend to the children.
- Then we pop the stack and proceed behind the unification code:

Once again the unification code for constructed terms:

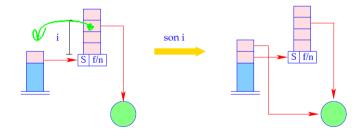
The instruction ustruct i implements the test of the root node of a structure:



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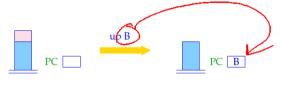


The instruction son i pushes the (reference to the) *i*-th sub-term from the structure pointed at from the topmost reference:



S[SP+1] = deref(H[S[SP]+i]); SP++;

It is the instruction up B which finally pops the reference to the structure:



SP--; PC = B;

The continuation address B is the next address after the build-section.

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f (p(f((a))))

Example:

For our example term $f(g(\bar{X},Y),a,Z)$ and $\rho = \{X \mapsto 1, Y \mapsto 2, Z \mapsto 3\}$ we obtain:

ustruct f/3 A_1	up B_2 B_2 :	son 2	putvar 2
son 1		uatom a	putstruct g/2
ustruct $g/2 A_2$ A_2 :	check 1	son 3	putatom a
son 1	putref 1	uvar 3	putvar 3
uref 1	putvar 2	up B_1	putstruct f/3
son 2	putstruct $g/2$ A_1 :	check 1	bind
uvar 2	bind	putref 1 B_1 :	

Code size can grow quite considerably — for deep terms. In practice, though, deep terms are "rare" :-)

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31 Clauses

Clausal code must

- allocate stack space for locals;
- evaluate the body;
- free the stack frame (whenever possible :-)

Let r denote the clause:

$$p(X_1,\ldots,X_k) \leftarrow g_1,\ldots,g_n.$$

Let $\{X_1, \dots, X_m\}$ denote the set of locals of r and ρ the address environment:

$$\rho X_i = i$$

Remark: The first *k* locals are always the formals :-)

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son 1	putref 1		uvar 3	putvar 3
uref 1	putvar 2		up B_1	putstruct f/3
son 2	putstruct g/2 A	l ₁ :	check 1	bind
uvar 2	bind		putref 1 B_1 :	

Code size can grow quite considerably — for deep terms. In practice, though, deep terms are "rare" :-)

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Then we translate:

```
\operatorname{code}_{\mathbb{C}} r = \operatorname{pushenv} \mathfrak{m} // allocates space for locals \operatorname{code}_{\mathbb{G}} g_1 \ \rho ... \operatorname{code}_{\mathbb{G}} g_n \ \rho popenv
```

The instruction popenv restores FP and PC and tries to pop the current stack frame.

It should succeed whenever program execution will never return to this stack frame :-)

The instruction pushenv m sets the stack pointer:



SP = FP + m;

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Example:

Consider the clause *r*:

$$\mathsf{a}(X,Y) \leftarrow \mathsf{f}(\bar{X},X_1), \mathsf{a}(\bar{X}_1,\bar{Y})$$

Then $code_C r$ yields:



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32 Predicates

A predicate q/k is defined through a sequence of clauses $rr\equiv r_1\dots r_f$. The translation of q/k provides the translations of the individual clauses r_i . In particular, we have for f=1:

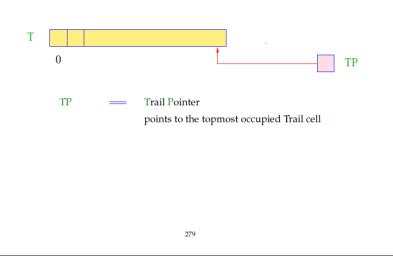
$$code_P rr = code_C r_1$$

If q/k is defined through several clauses, the first alternative must be tried. On failure, the next alternative must be tried

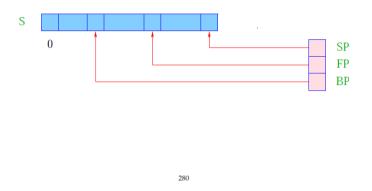
⇒ backtracking :-)

32.1 Backtracking

- Whenever unifcation fails, we call the run-time function backtrack().
- In order to undo intermediate variable bindings, we always have recorded new bindings with the run-time function trail().
- The run-time function trail() stores variables in the data-structure trail:



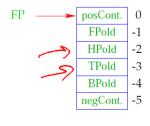
The current stack frame where backtracking should return to is pointed at by the extra register BP:



A backtrack point is stack frame to which program execution possibly returns.

- We need the code address for trying the next alternative (negative continuation address);
- We save the old values of the registers HP, TP and BP.
- Note: The new BP will receive the value of the current FP :-)

For this purpose, we use the corresponding four organizational cells:

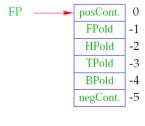


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- Note: The new BP will receive the value of the current FP :-)

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For more comprehensible notation, we thus introduce the macros:

```
\begin{array}{lll} \operatorname{posCont} & \equiv & S[\operatorname{FP}] \\ \operatorname{FPold} & \equiv & S[\operatorname{FP}-1] \\ \operatorname{HPold} & \equiv & S[\operatorname{FP}-2] \\ \operatorname{TPold} & \equiv & S[\operatorname{FP}-3] \\ \operatorname{BPold} & \equiv & S[\operatorname{FP}-4] \\ \operatorname{negCont} & \equiv & S[\operatorname{FP}-5] \end{array}
```

for the corresponding addresses.

Remark:

```
Occurrence on the left == saving the register

Occurrence on the right == restoring the register
```

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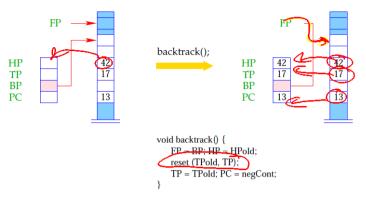
```
\operatorname{code}_{P} rr = \operatorname{q/k}: \operatorname{setbtp} 
\operatorname{try} A_{1}
\ldots
\operatorname{try} A_{f-1}
\operatorname{delbtp}
\operatorname{jump} A_{f}
A_{1}: \operatorname{code}_{\mathbb{C}} r_{1}
```

Note:

- We delete the backtrack point before the last alternative :-)
- We jump to the last alternative never to return to the present frame :-))

 A_f : code_C r_f

Calling the run-time function void backtrack() yields:



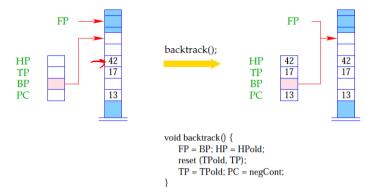
where the run-time function <code>reset()</code> undoes the bindings of variables established since the backtrack point.

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```
Functions void trail(ref u) and void reset (ref y, ref x) can thus be implemented as:
```

Here, S[BP-2] represents the heap pointer when creating the last backtrack point.

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where the run-time function <code>reset()</code> undoes the bindings of variables established since the backtrack point.

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32.3 Wrapping it Up

Assume that the predicate q/k is defined by the clauses r_1,\ldots,r_f (f>1). We provide code for:

- setting up the backtrack point;
- · successively trying the alternatives;
- deleting the backtrack point.

This means:

Functions $\mbox{\ \ void\ trail(ref\ u)\ \ and\ \ \ }\mbox{\ \ void\ reset\ (ref\ y,\ ref\ x)\ \ }\mbox{\ \ can}$ thus be implemented as:

```
void trail (ref u) {
  if (u < S[BP-2]) {
    for (ref u=y; x<u; u--)
    TP = TP+1;
    T[TP] = u;
  }
}</pre>
```

Here, S[BP-2] represents the heap pointer when creating the last backtrack point.

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```
code_{p} rr = q/k : 
try A_{1}
...
try A_{f-1}
delbtp
jump A_{f}
A_{1} : code_{C} r_{1}
...
A_{f} : code_{C} r_{f}
```

Note:

- We delete the backtrack point before the last alternative :-)
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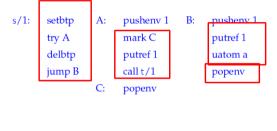
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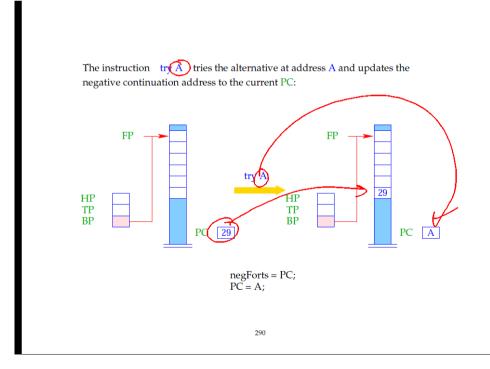
$$s(X) \leftarrow t(\bar{X})$$

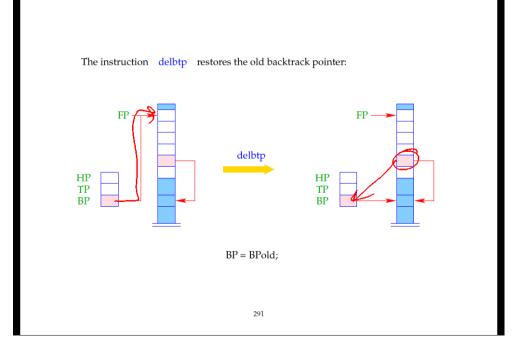
 $s(X) \leftarrow \bar{X} = a$

The translation of the predicate s yields:



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32.4 Popping of Stack Frames

Recall the translation scheme for clauses:

```
code_C r = pushenv m
code_G g_1 \rho
...
code_G g_n \rho
popenv
```

The present stack frame can be popped ...

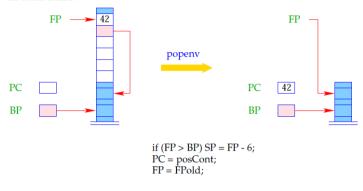
- if the applied clause was the last (or only); and
- if all goals in the body are definitely finished.
 - \implies the backtrack point is older :-)

 \Longrightarrow FP > BP

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The instruction popenv restores the registers FP and PC and possibly pops the stack frame:



Warning: popenv may fail to de-allocate the frame !!!