

Script generated by TTT

Title: Simon: Compilerbau (26.05.2014)

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Topic:

Semantic Analysis

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Semantic Analysis

Scanner and parser accept programs with correct syntax.

- not all programs that are syntactically correct make sense

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 - the language definition defines what erroneous means

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 - find possibilities to "optimize" the program
 - warn about possibly incorrect programs.

$c \&\& (a == b)$
 $\text{if } (a == b) \{$

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Semantic Analysis

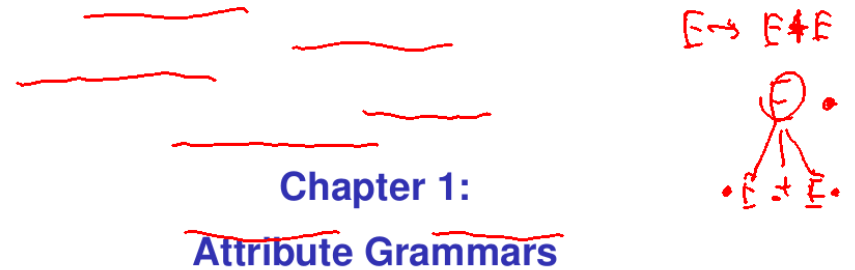
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~> a semantic analysis annotates the syntax tree with attributes

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Semantic Analysis



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Attribute Grammars

- many computations of the semantic analysis as well as the code generation operate on the syntax tree
- what is computed at a given node only depends on the *type* of that node (which is usually a non-terminal)
- we call this a *local* computation:
 - only accesses already computed information from neighbouring nodes
 - computes new information for the current node and other neighbouring nodes

$$E \rightarrow E + E$$

Definition attribute grammar

An **attribute grammar** is a **CFG** extended by

- an set of attributes for each non-terminal and terminal
- local attribute equations

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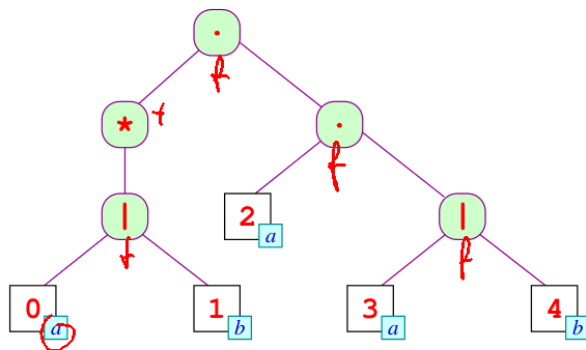
- an set of attributes for each non-terminal and terminal
- local attribute equations

- in order to be able to evaluate the attribute equations, all attributes mentioned in that equation have to be evaluated already
 \leadsto the nodes of the syntax tree need to be visited in a certain *sequence*

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Example: Computation of the $\text{empty}[r]$ Property

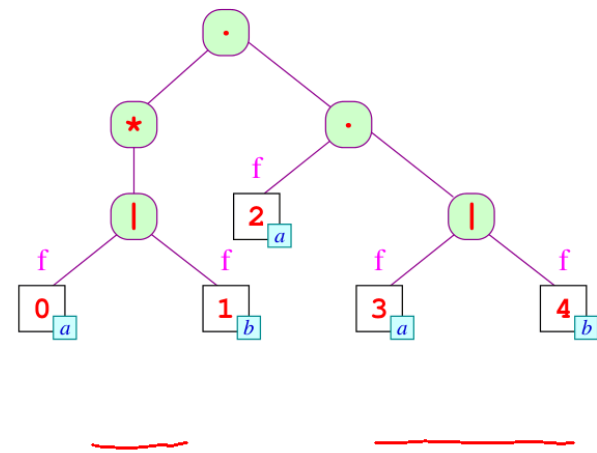
Consider the syntax tree of the regular expression $(a|b)^*a(a|b)$:



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Implementation Strategy

- attach an attribute empty to every node of the syntax tree
- compute the attributes in a depth-first traversal:
 - at a leaf, we can compute the value of empty without considering other nodes
 - the attribute of an inner node only depends on the attribute of its children
- the empty attribute is a synthetic attribute
- it may be computed by a pre- or post-order traversal

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in general:

Definition

An attribute is called

- synthetic if its value is always propagated upwards in the tree (in the direction leaf \rightarrow root)
- inherited if its value is always propagated downwards in the tree (in the direction root \rightarrow leaf)

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Attribute Equations for empty

In order to compute an attribute locally, we need to specify attribute equations for each node.

These equations depend on the type of the node:

$$\begin{array}{l} \tau \mapsto x \\ \text{for leaves: } r \equiv [i \ x] \quad \text{we define } \text{empty}[r] = (x \equiv \epsilon). \\ \text{otherwise: } \\ \tau \rightarrow r_1 \mid r_2 \quad \begin{array}{l} \text{empty}[r_1 \mid r_2] = \text{empty}[r_1] \vee \text{empty}[r_2] \\ \text{empty}[r_1 \cdot r_2] = \text{empty}[r_1] \wedge \text{empty}[r_2] \\ \text{empty}[r_1^*] = t \\ \text{empty}[r_1?] = t \end{array} \end{array}$$

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Specification of General Attribute Systems

The empty attribute is synthetic, hence, the equations computing it can be given using structural induction.

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Specification of General Attribute Systems

The **empty** attribute is *synthetic*, hence, the equations computing it can be given using *structural induction*.

In general, attribute equations combine information for children and parents.

- \leadsto need a more flexible way to specify attribute equations that allows mentioning of parents and children
- use consecutive indices to refer to neighbouring attributes

$\text{empty}[0]$: the attribute of the current node $\underline{E} \mapsto \underline{E + E}$
 $\text{empty}[i]$: the attribute of the i -th child ($i > 0$)

... in the example:

$\gamma \rightarrow \gamma | \gamma$
 $\gamma \rightarrow \gamma *$

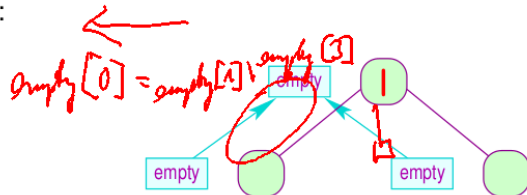
x	:	$\text{empty}[0]$:=	$(x \equiv \epsilon)$
$ $:	$\text{empty}[0]$:=	$\text{empty}[1] \vee \text{empty}[2]$
\cdot	:	$\text{empty}[0]$:=	$\text{empty}[1] \wedge \text{empty}[2]$
$*$:	$\text{empty}[0]$:=	t
$?$:	$\text{empty}[0]$:=	t

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Observations

- the *local* attribute equations need to be evaluated using a *global* algorithm that knows about the dependencies of the equations
- in order to construct this algorithm, we need
 - 1 a sequence in which the nodes of the tree are visited
 - 2 a sequence within each node in which the equations are evaluated
- this *evaluation strategy* has to be compatible with the *dependencies* between attributes

We illustrate dependencies between attributes using directed graph edges:



\leadsto arrow points in the direction of information flow

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Observations

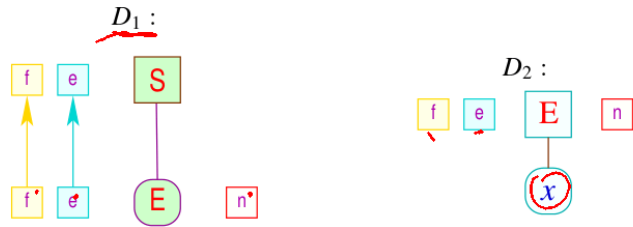
- in order to infer an *evaluation strategy*, it is not enough to consider the *local* attribute dependencies at each node
- the evaluation strategy must also depend on the *global* dependencies, that is, on the information flow between nodes
- the global dependencies thus change with each new abstract syntax tree
- in the example, the information flows always from the children to the parent node
 \leadsto a depth-first post-order traversal is possible
- in general, variable dependencies can be much more complicated

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Simultaneous Computation of Multiple Attributes

Compute empty, first, next of regular expression:

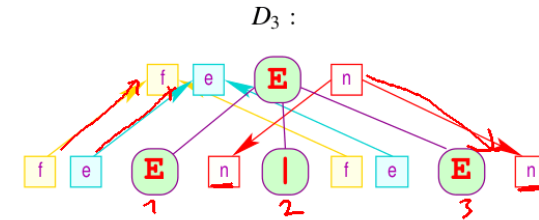
$$\begin{aligned}
 1 \quad \boxed{S \rightarrow E} &: \quad \text{empty}[0] := \text{empty}[1] \\
 &\quad \text{first}[0] := \text{first}[1] \\
 &\quad \text{next}[1] := \emptyset \\
 2 \quad \boxed{E \rightarrow x} &: \quad \text{empty}[0] := (x \equiv \epsilon) \\
 &\quad \text{first}[0] := \{x \mid x \neq \epsilon\} \\
 &\quad // \text{ (no equation for next) }
 \end{aligned}$$



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Regular Expressions: Rules for Alternative

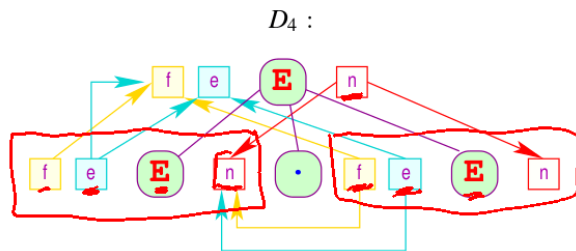
$$\begin{aligned}
 3 \quad \boxed{E \rightarrow E|E} &: \quad \text{empty}[0] := \text{empty}[1] \vee \text{empty}[2] \\
 &\quad \text{first}[0] := \text{first}[1] \cup \text{first}[2] \\
 &\quad \text{next}[1] := \text{next}[0] \\
 &\quad \text{next}[2] := \text{next}[0]
 \end{aligned}$$



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Regular Expressions: Rules for Concatenation

$$\begin{aligned}
 \boxed{E \rightarrow E \cdot E} &: \quad \text{empty}[0] := \text{empty}[1] \wedge \text{empty}[2] \\
 &\quad \text{first}[0] := \text{first}[1] \cup (\text{empty}[1] ? \text{first}[2] : \emptyset) \\
 &\quad \text{next}[1] := \text{first}[2] \cup (\text{empty}[2] ? \text{next}[0] : \emptyset) \\
 &\quad \text{next}[2] := \text{next}[0]
 \end{aligned}$$



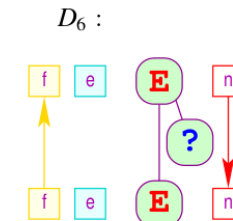
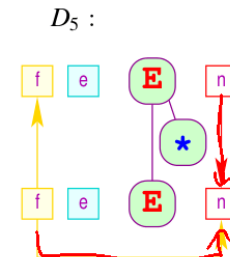
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Regular Expressions: Kleene-Star and '?'

$$\begin{aligned}
 \boxed{E \rightarrow E^*} &: \quad \text{empty}[0] := t \\
 &\quad \text{first}[0] := \text{first}[1] \cup \text{first}[1] \cup \{\text{empty}[1]\} \\
 &\quad \text{next}[1] := \text{first}[1] \cup \text{next}[0]
 \end{aligned}$$

Handwritten note: first[1] ∪ {empty[1]} next[0]

$$\begin{aligned}
 \boxed{E \rightarrow E?} &: \quad \text{empty}[0] := t \\
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Challenges for General Attribute Systems

- assume that the grammar Gr has no useless productions
- let \mathcal{T} denote all derivable syntax trees of Gr
- an evaluation strategy can only exist if for *any* abstract syntax tree $t \in \mathcal{T}$, the dependencies between attributes are **acyclic**

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Consider the 6 productions of the regular expression grammar:

D_i	1	$S \rightarrow E$	4	$E \rightarrow E \cdot E$
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Idea: Compute a directed graph D'_i for each production i .

- the vertices of D'_i are its lhs attributes $a_1[0], \dots, a_n[0]$
- an edge $a_i[0] \rightarrow a_j[0]$ indicates $a_i[0]$ must be evaluated so that visiting the production can compute $a_j[0]$
- for productions whose rhs only contains terminals $D'_i = D_i$
- compute new edges for other productions based on the current edges of its rhs non-terminals (\rightsquigarrow next slide)
- when no new edges can be added, the graphs D'_i denote the dependencies of all possible derivation trees
- no. of edges in each graph is finite \rightsquigarrow termination guaranteed

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Computing Dependencies $i: N \rightarrow N_1 \dots N_m$

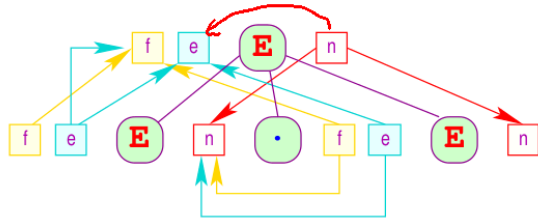
Define $D'_i[G_1, \dots, G_n]$ to be the graph obtained from D'_i by adding an edge from $a_i[0]$ to $a_j[0]$ if there is a path from $a_i[0]$ to $a_j[0]$ in the dependency graph D_i where graphs G_j give the dependencies for the corresponding rhs-attributes. Abort when cycles exist.

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Example: $D'_4[G_1, G_2, G_3]$: Dependency graph of D_4 :



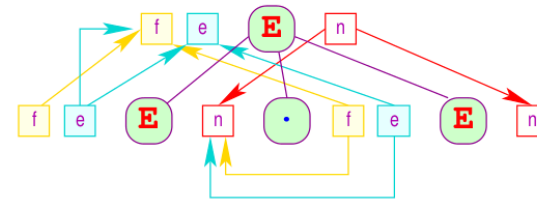
Suppose graph G_2 is empty and graphs G_1 and G_3 are as follows:



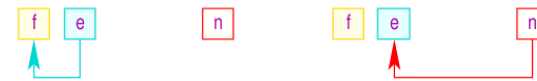
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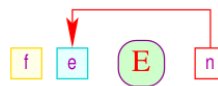
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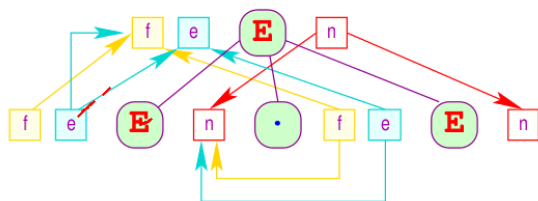
Edges added to D'_4 :



Computing Dependencies

Define $D'_i[G_1, \dots, G_n]$ to be the graph obtained from D'_i by adding an edge from $a_i[0]$ to $a_j[0]$ if there is a path from $a_i[0]$ to $a_j[0]$ in the dependency graph D_i where graphs G_i give the dependencies for the corresponding rhs-attributes. Abort when cycles exists.

Example: $D'_4[G_1, G_2, G_3]$: Dependency graph of D_4 :



Suppose graph G_2 is empty and graphs G_1 and G_3 are as follows:



Edges added to D'_4 : Which edges are added for $D'_4[G_3, G_2, G_1]$?



Complexity of Computing Dependencies

p	rule	D'_p	p	rule	D'_p
1	$\underline{S} \rightarrow E$	$f[0] \ e[0]$	4	$E \rightarrow E \cdot E$	$f[0] \ e[0] \ n[0]$
2	$\underline{E} \rightarrow x$	$f[0] \ e[0] \ n[0]$	5	$E \rightarrow E^*$	$f[0] \ e[0] \ n[0]$
3	$\underline{E} \rightarrow E E$	$f[0] \ e[0] \ n[0]$	6	$E \rightarrow E^?$	$f[0] \ e[0] \ n[0]$

Add edges by repeatedly evaluating until stable:

- $\underline{D}'_1[G_1]$ for $G_1 \in \{D'_2, \dots, D'_6\}$
- $\underline{D}'_3[G_1, G_2, G_3]$ for $G_1, G_3 \in \{D'_2, \dots, D'_6\}, G_2$ empty
- $\underline{D}'_4[G_1, G_2, G_3]$ for $\underline{G}_1, \underline{G}_3 \in \{D'_2, \dots, D'_6\}, G_2$ empty
- $\underline{D}'_5[G_1, G_2]$ for $G_1 \in \{D'_2, \dots, D'_6\}, G_2$ empty
- $\underline{D}'_6[G_1, G_2]$ for $\underline{G}_1 \in \{D'_2, \dots, D'_6\}, G_2$ empty

Complexity of Computing Dependencies

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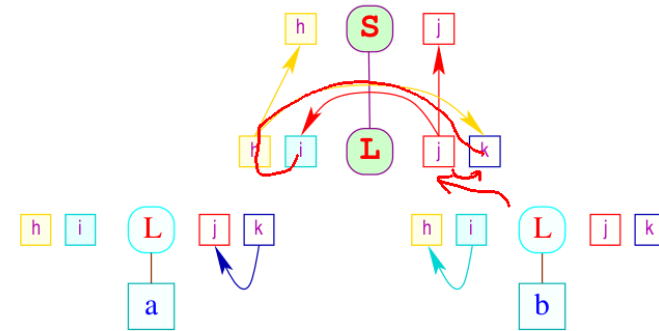
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- for n attributes, there are n^2 possible edges
- worst case: only one edge is added in each evaluation of D'_i
- checking that no cyclic attribute dependencies can arise is DEXPTIME-complete [Jazayeri, Odgen, Rounds, 1975] 2^n

Example: Checking Circularity

p	rule	D'_p
Grammar: 1	$S \rightarrow L$	$h[0] \quad j[0]$
2	$L \rightarrow a$	$h[0] \quad i[0] \quad j[0] \quad k[0]$
3	$L \rightarrow b$	$h[0] \quad i[0] \quad j[0] \quad k[0]$

Dependency graphs D_p :



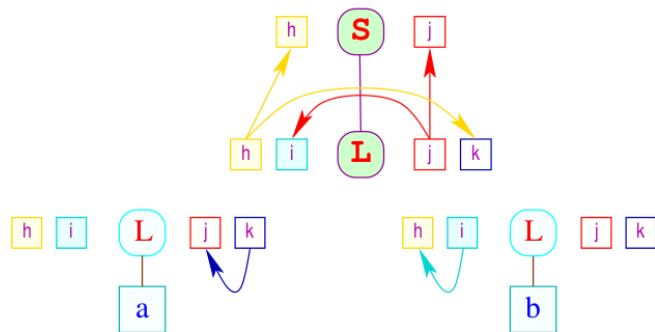
Apply until stable:

$$D'_1[G_1] \quad \text{for } G_1 \in \{D'_2, D'_3\}$$

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Dependency graphs D_p :



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Strongly Acyclic Attribute Dependencies

Problem: with larger grammars, this algorithm is too expensive
Goal: find a sufficient condition for an attribute system to be acyclic

Strongly Acyclic Attribute Dependencies

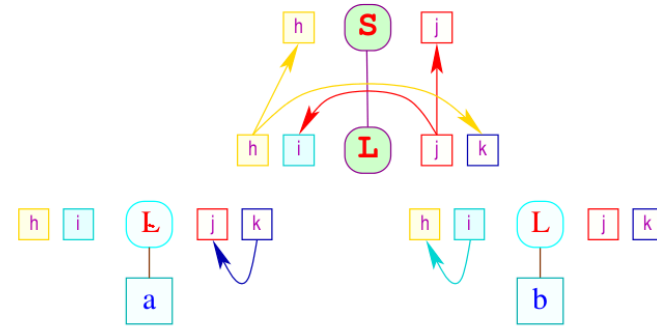
Problem: with larger grammars, this algorithm is too expensive
Goal: find a *sufficient* condition for an attribute system to be acyclic

Idea: Compute dependency graph D'_s for each non-terminal $s \in N$.

- for all productions $N \rightarrow t_1 \dots t_n$ with t_i terminals:
 $D'_N = D_{i_1} \cup \dots \cup D_{i_k}$ where i_1, \dots, i_k are the productions indices
- compute $D'_N[G_1, \dots, G_n]$ for each production $N \rightarrow s_1 \dots s_n$ where G_i is the graph between $a_{i_1}[0], \dots, a_{i_k}[0]$ of s_i
- re-evaluate each rule until none of the graphs change anymore
- if a cycle is detected during the computation of D'_N , report "may have cycle"

Example: Strong Acyclic Test

Consider again the grammar $S \rightarrow L, L \rightarrow a \mid b$. Dependency graphs D_p :

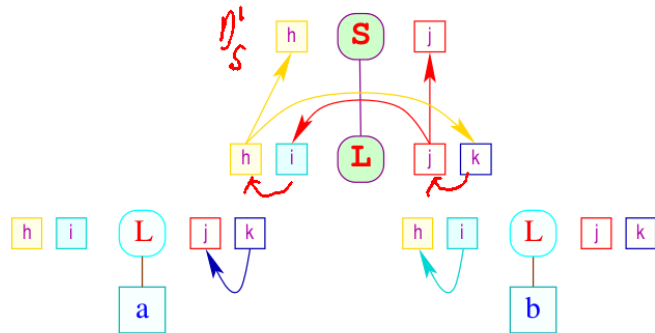


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p	rule	N	D'_N
1	$S \rightarrow L$	S	$h[0] \quad j[0]$
2	$L \rightarrow a$	L	$h[0] \leftarrow i[0] \quad j[0] \leftarrow k[0]$
3	$L \rightarrow b$	L	$h[0] \leftarrow i[0] \quad j[0] \leftarrow k[0]$

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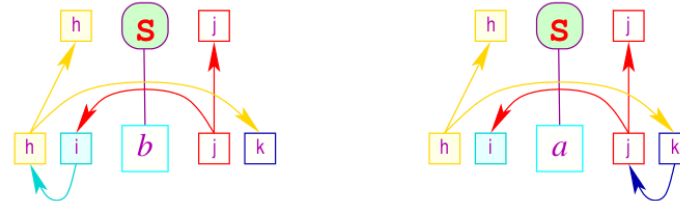


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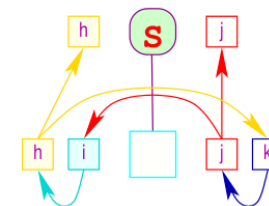
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Strong Acyclic and Acyclic

The grammar $S \rightarrow L, L \rightarrow a \mid b$ has only two derivation trees which are both acyclic:



It is not strongly acyclic since the dependence graph for the non-terminal L has a cycle when computing D'_s :



From Dependencies to Evaluation Strategies

Possible strategies:

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- let the user define the evaluation order

From Dependencies to Evaluation Strategies

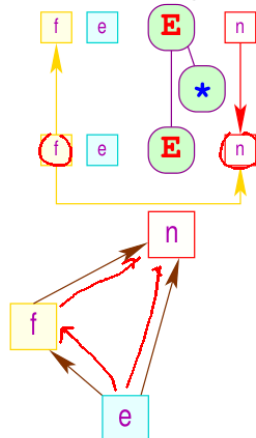
Possible strategies:

- let the user define the evaluation order
- automatic strategy based on the dependencies:
 - use local dependencies to determine which attributes to compute

- suppose we require $s[1]$
- computing $s[1]$ requires $f[1]$
- $f[1]$ depends on an attribute in the child, so descend

- compute attributes in passes

- compute a dependency graph between attributes (no go if cyclic)
- traverse AST once for each attribute; here three times, once for e, f, g
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From Dependencies to Evaluation Strategies

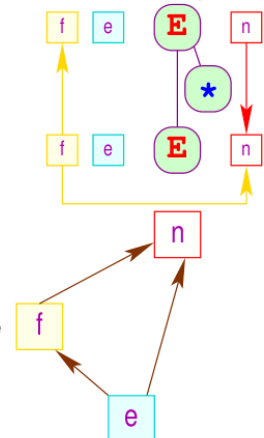
Possible strategies:

- let the user define the evaluation order
- automatic strategy based on the dependencies:
 - use local dependencies to determine which attributes to compute

- suppose we require $s[1]$
- computing $s[1]$ requires $f[1]$
- $f[1]$ depends on an attribute in the child, so descend

- compute attributes in passes

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- consider a fixed strategy and only allow an attribute system that can be evaluated using this strategy

Linear Order from Dependency Partial Order

Possible *automatic* strategies:



Linear Order from Dependency Partial Order

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1 demand-driven evaluation

- start with the evaluation of any required attribute
- if the equation for this attribute relies on as-of-yet unevaluated attributes, compute these recursively
- \rightsquigarrow visits the nodes of the syntax tree on demand
- (following a dependency on the parent requires a pointer to the parent)

2 evaluation in passes

- *minimize* the number of *visits* to each node
- organize the evaluation of the tree in passes
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consider example for *demand-driven* evaluation

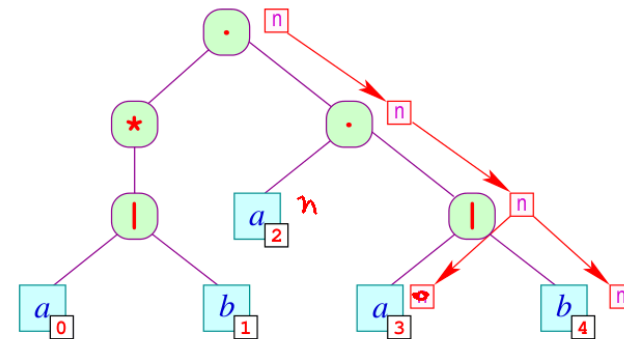


Example for Demand-Driven Evaluation

Compute *next* at the leaves of $a(a|b)$ in the expression $((a|b)*a(a|b))$:

$$\boxed{|} : \begin{array}{l} \text{next}[1] := \text{next}[0] \\ \text{next}[2] := \text{next}[0] \end{array}$$

$$\boxed{\cdot} : \begin{array}{l} \text{next}[1] := \text{first}[2] \cup (\text{empty}[2] ? \text{next}[0] : \emptyset) \\ \text{next}[2] := \text{next}[0] \end{array}$$

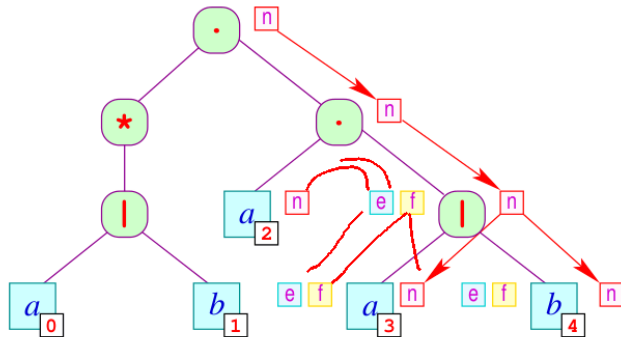


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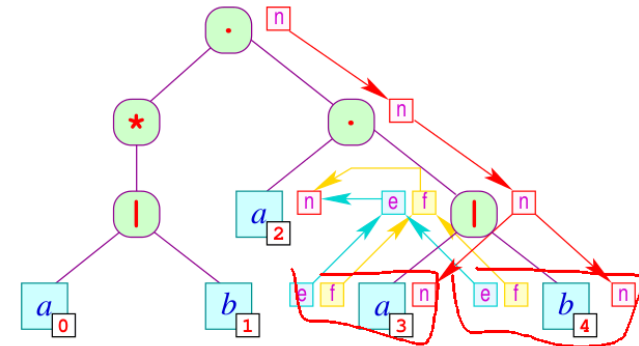
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Demand-Driven Evaluation

Observations

- only required attributes are evaluated
- the evaluation sequence depends – in general – on the actual syntax tree
- the algorithm must track which attributes it has already evaluated
- the algorithm may visit nodes more often than necessary
- each node must contain a pointer to its parent
- the algorithm is not local

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~> perform evaluation in **passes**

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Evaluation in Passes

Idea: traverse the syntax tree several times; each time, evaluate all those equations $a[i_a] = f(b[i_b], \dots, z[i_z])$ whose arguments $b[i_b], \dots, z[i_z]$ are known

For a **strongly acyclic attribute system**:

- the local dependencies in D_i of the i th production $N \rightarrow s_1 \dots s_n$ together the dependencies D'_i for each s_i define a sequence in which attributes can be evaluated
- determine a sequence in which the children are visited so that as many attributes as possible are evaluated
- in each pass at least one new attribute is evaluated
- requires at most n passes for evaluating n attributes
- since a traversal strategy exists for evaluating one attribute, it might be possible to find a strategy to evaluate more attributes ~> **optimization problem**
- **note:** evaluating attribute set $\{a_{i_1}[0] \dots a_{i_m}[0]\}$ for rule $N \rightarrow \dots N \dots$ may evaluate a different attribute set of its children ~> **up to $2^k - 1$ evaluation functions for N**

... in the example:

- **empty** and **first** can be computed together
- **next** must be computed in a separate pass

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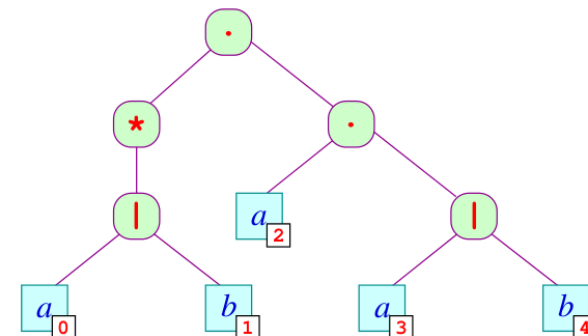
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Implementing State

Problem: In many cases some sort of state is required.

Example: numbering the leafs of a syntax tree



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